

# Assessing the Performance of qpAdm: A Statistical Tool for Studying Population Admixture

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## ABSTRACT

qpAdm is a statistical tool for studying the ancestry of populations with histories that involve admixture between two or more source populations. Using qpAdm, it is possible to identify plausible models of admixture that fit the population history of a group of interest and to calculate the relative proportion of ancestry that can be ascribed to each source population in the model. Although qpAdm is widely used in studies of population history of human (and non-human) groups, relatively little has been done to assess its performance. We performed a simulation study to assess the behavior of qpAdm under various scenarios in order to identify areas of potential weakness and establish recommended best practices for use. We find that qpAdm is a robust tool that yields accurate results in many cases, including when data coverage is low, there are high rates of missing data or ancient DNA damage, or when diploid calls cannot be made. However, we caution against co-analyzing ancient and present-day data, the inclusion of an extremely large number of reference populations in a single model, and analyzing population histories involving extended periods of gene flow. We provide a user guide suggesting best practices for the use of qpAdm.

36

## INTRODUCTION

37 The last decade has experienced a revolution in the amount of genetic data available to study  
38 from both living and ancient organisms. Questions about the origins of populations have  
39 increased in complexity, often in an effort to understand histories that involve admixture, which  
40 are incompatible with traditional tree-like models of relatedness. qpAdm is a tool that can be  
41 used to understand the history of admixed populations. It has been applied to study the genetic  
42 history of human populations that would otherwise remain mysterious. For instance, the use of  
43 qpAdm was vital to studying the ancestry of the Late Bronze Age Greek culture of the  
44 “Mycenaeans” (LAZARIDIS *et al.* 2017)—the subjects of the Iliad and Odyssey. However, little has  
45 been done to assess qpAdm’s performance under both simple and complex scenarios.

46 A potential drawback of many population genetic tools for studying the population history of  
47 specific groups (PATTERSON *et al.* 2012; PICKRELL AND PRITCHARD 2012) is that they require the  
48 historical relationships of all other populations included in the analysis to be explicitly modeled.  
49 This underlying phylogeny is either specified by the user (as in qpGraph) or is calculated during  
50 the analysis (as in TreeMix). This may lead to biases or errors in inferences about admixture if  
51 mistakes are made when specifying the underlying relationships of non-target populations  
52 (LIPSON 2020). This requirement for a complete and accurate population history is especially  
53 difficult to satisfy in studies that utilize ancient DNA, which increasingly attempt to use genetic  
54 data of limited quality to analyze nuanced differences between closely related groups. However,  
55 even in cases where it is difficult to reconstruct a full population history, it is often possible to  
56 examine patterns of shared genetic drift between various populations in order to learn about

57 their relationship relative to one another (PATTERSON *et al.* 2012). qpAdm exploits this  
58 information, enabling admixture models to be tested for plausibility and admixture proportions  
59 to be estimated.

60 The theory underlying qpAdm, which was introduced in HAAK *et al.* (2015), builds upon a class of  
61 statistics known as *f*-statistics (PATTERSON *et al.* 2012). *f*-statistics analyze patterns of allele  
62 frequency correlations among populations in order to determine whether their population  
63 histories can be described using strictly tree-based models, or if more complex models, such as  
64 those involving admixture, are required to explain the genetic data. *f*-statistics have been widely  
65 used in the population genetic literature and their behavior is well understood (REICH *et al.* 2009;  
66 PATTERSON *et al.* 2012; PETER 2016; SORAGGI AND WIUF 2019; LIPSON 2020). qpAdm harnesses the  
67 power of *f*-statistics to determine whether a population of interest (a target population) can be  
68 plausibly modeled as descending from a common ancestor of one or more source populations.  
69 For example, in a model with two source populations, qpAdm tests whether the target population  
70 is the product of a two-way admixture event between these source populations. The method  
71 requires a list of target and source populations and a list of additional reference populations  
72 which provide information about the relationships among the target and source populations.

73 The target and source populations are collectively referred to as ‘left’ populations, due to their  
74 position as the left-most arguments in the  $f_4$ -statistics involved in the calculations. Additionally,  
75 users must specify a set of ‘right’ populations that serve as references against which the  
76 relationships of the target and source populations are considered. Previously, ‘right’ populations  
77 were referred to as ‘outgroup’ populations, but we avoid this term because it suggests that

78 reference populations should be outgroups in phylogenetic sense (i.e. equally closely related to  
79 all 'left' populations). In fact, if all 'right' populations are symmetrically related to all 'left'  
80 populations in this way, qpAdm will not produce meaningful results. The method requires  
81 differential relatedness, meaning that at least some 'right' populations must be more closely  
82 related to a subset of 'left' populations than to the other 'left' populations. We illustrate this  
83 further in Methods & Results.

84 qpAdm computes a matrix of  $f$ -statistics of all possible pairs of populations in the 'left' and 'right'  
85 sets, of the form  $f_4(\text{Left}_i, \text{Left}_j; \text{Right}_k, \text{Right}_l)$ . If the source populations are descended from  $n$   
86 different ancestral populations, then the matrix of  $f$ -statistics will have a rank (a maximum  
87 number of linearly independent allele-frequency vectors) equal to  $n-1$  (HAAK *et al.* 2015). We note  
88 that if all  $f_4$ -statistics are computed from the same set of SNPs, which is the default mode of  
89 qpAdm, a basis for the statistics can be found using a matrix of reduced dimension, specifically  
90 by fixing both the target population ( $\text{Left}_i$  above) and  $\text{Right}_k$ . This also improves the efficiency of  
91 the covariance calculations. qpAdm accounts for correlations between neighboring alleles and  
92 between related populations, measuring covariance using a block jackknife. For each model, it  
93 gives a p-value which is used to determine whether the proposed admixture model is plausible.  
94 The p-value is calculated using a likelihood ratio test comparing a constrained null model to an  
95 unconstrained alternative model. Specifically, it tests whether including the target population in  
96 the 'left' populations requires an additional independent ancestral population (i.e. changes the  
97 rank of the matrix of  $f$ -statistics from  $n-1$  to  $n$ ). A simple example in which this would be required,  
98 and the constrained model would be rejected, is when the putative target population is actually

99 an outgroup to all source populations. In the constrained model, the admixed ancestral  
100 population of the target population is a mixture of sources.

101 While qpAdm has been theoretically described (HAAK *et al.* 2015) and applied in numerous studies  
102 (e.g. LAZARIDIS *et al.* 2016; HABER *et al.* 2017; LAZARIDIS *et al.* 2017; SKOGLUND *et al.* 2017; DE BARROS  
103 DAMGAARD *et al.* 2018a; DE BARROS DAMGAARD *et al.* 2018b; HAJDINJAK *et al.* 2018; HARNEY *et al.* 2018;  
104 NARASIMHAN *et al.* 2018; OLALDE *et al.* 2018), producing results that are consistent with those of  
105 other population genetic methods, very little has been done to assess the performance of the  
106 tool when the population history is known (i.e. using simulated data). The only simulation-based  
107 analysis that has been previously conducted examined whether simulated populations—  
108 generated according to the model fitted by qpAdm, by resampling data using the source  
109 populations and estimated admixture proportions—behaved similarly to the real target  
110 population in further statistical analyses (LAZARIDIS *et al.* 2017). Although this limited example  
111 supports the use of qpAdm in population genetic analyses, it did not address any of the potential  
112 limitations of the method. Here we use simulated genomic data to study the distributions of p-  
113 values and estimated admixture proportions from qpAdm, the potential of qpAdm to distinguish  
114 optimal from non-optimal models of admixture for a given set of samples, and the performance  
115 of qpAdm in the face of more challenging demographic scenarios.

116 The chief purpose of qpAdm is to identify a subset of plausible models of a population's ancestry  
117 from a larger set of possible models. Models are deemed implausible if they are rejected (by  
118 having a small p-value) or if their estimated admixture proportions fall outside the biologically  
119 relevant range (0,1). Thus, p-values are applied in a non-standard statistical way. Users propose

120 a range of possible models, in which they attempt to model the target population using a variety  
121 of different combinations of populations as sources, then eliminate implausible models. The set  
122 of plausible models are the ones which are *not* rejected, meaning they have p-values *greater*  
123 than the chosen significance level, which is usually 5%. To illustrate, Box 1 describes how an  
124 analogous technique might be applied to identify plausible values of the (unknown) probability  
125 of heads for a coin.

126 Identical to standard statistical methods, this approach will work best when the p-values  
127 generated by qpAdm follow a uniform distribution, if the correct admixture model is specified.  
128 Then the correct model will be rejected 5% of the time when a threshold of  $p < 0.05$  is applied.  
129 For other plausible but less-optimal models, the distribution of p-value is not expected to be  
130 uniform but should have an appreciable chance of being above the 5% cutoff. The distribution of  
131 p-values for implausible or incorrect models should fall largely below the 5% cutoff. While  
132 experience suggests that the p-values generated by qpAdm are reasonably consistent with these  
133 expectations, in this work we perform the first systematic test of these ideas.

**Box 1. Coin flipping analogy.**

Imagine that we wish to know which of several possible models (here values,  $p_0$ ) of the probability of heads best describes the behavior of a coin. The actual value is unknown and the coin may be unfair. To mimic what is done in qpAdm, we might specify a set of possible models, for instance with probabilities of heads equal to 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, or 0.9. To determine which of the possible models are plausible for the coin, we flip it multiple times and count the number of heads we observe. The probability of observing that number of heads under each of the possible models would be given by the binomial distribution. Again by analogy with qpAdm, we could assess the plausibility of each model by a generalized likelihood ratio test of each null model against the unconstrained alternative.

If we flip the coin 10 times, and it lands on heads 7 times, using a p-value threshold of 0.05, we can already eliminate 0.1-0.4 and 0.9 as potential models of the probability of heads for our coin (Table 1.1). By increasing the number of flips to 100, if we observe 73 heads, we can further eliminate 0.5 and 0.6, leaving only 0.7 and 0.8 as plausible models for the probability of heads of the coin. As with this analogy, qpAdm identifies a set of plausible models by not rejecting null hypotheses (possibly by what would be Type II error in a standard statistical test).

Note that in this coin flipping analogy, any model which did not have the exactly correct probability of heads would eventually be rejected if enough data were collected. Our findings in the main text suggest that this particular problem is not an issue for qpAdm, which specifies models in a different way and which admits a range of similar, plausible models even using whole-genome data.

Models ( $p_0$ ) for the probability of heads	P-values from a generalized likelihood ratio test of $H_0:p=p_0$ against the unconstrained alternative	
	Number of flips	Number of heads
	10	100
	7	73
0.1	< 0.001	< 0.001
0.2	< 0.001	< 0.001
0.3	< 0.001	< 0.001
0.4	0.007	< 0.001
0.5	0.070	< 0.001
0.6	0.353	0.006
0.7	1.000	0.508
0.8	0.289	0.092
0.9	0.013	< 0.001

**Table 1.1** Using a generalized likelihood-ratio test of  $H_0:p=p_0$  to identify plausible models for the probability of heads of a coin. Models that produce p-values greater or equal to 0.05 are highlighted in blue, while those that are less than 0.05 are highlighted in red.

135 Similarly, although the estimated admixture proportions calculated by qpAdm appear generally  
136 consistent with values generated using other statistics, the accuracy of these estimates have  
137 never been rigorously tested. Of particular interest is the accuracy of these estimates when  
138 calculated on low quality data, as qpAdm is often applied to the study of ancient DNA, which is  
139 characteristically low coverage, may have a high rate of missing data, and is susceptible to  
140 deamination of cytosine nucleotides (manifesting in sequence data as cytosines being misread  
141 as thymines). Further, ancient DNA is often subject to a complex ascertainment process that  
142 could potentially bias statistical analyses. We explore the impact of each of these factors on the  
143 admixture proportions estimated by qpAdm.

144 Additionally, while one of the main features of qpAdm is its ability to distinguish between optimal  
145 and non-optimal models for a group's population history, there are no formal recommendations  
146 about what strategy should be employed to compare models. We therefore consider two of the  
147 most commonly employed strategies for model comparison, highlighting their potential benefits  
148 and weaknesses.

149 Finally, we conclude by exploring non-standard cases where the expected behavior of qpAdm is  
150 poorly understood, such as the impact of including a large number of populations in the reference  
151 population set and the behavior of qpAdm when applied to population histories that involve  
152 continuous gene flow rather than single pulses of admixture.

153 We show that qpAdm reliably identifies population histories involving admixture and accurately  
154 infers admixture proportions. It is robust to low coverage, high rates of missing data, DNA  
155 damage (when occurring at similar rates in all populations), the use of pseudo-haploid data, small



156 sample size, and ascertainment bias. We also identify some issues with naive applications of  
157 qpAdm. One of these issues is that multiple plausible scenarios may be found most of which are  
158 not the truth because qpAdm uses non-rejection of null models as its criterion for plausibility.  
159 Another of these issues is that true models may be rejected if samples from too many populations  
160 are included in the analysis. A third is that qpAdm results may be difficult to interpret and even  
161 misleading under conditions of continuous gene flow. In order to help guard against these  
162 potential pitfalls and make this tool more accessible to users, we include an updated user guide  
163 for qpAdm (Supplementary Materials 1) and make specific recommendations for best practices  
164 for use.

## 165 METHODS & RESULTS

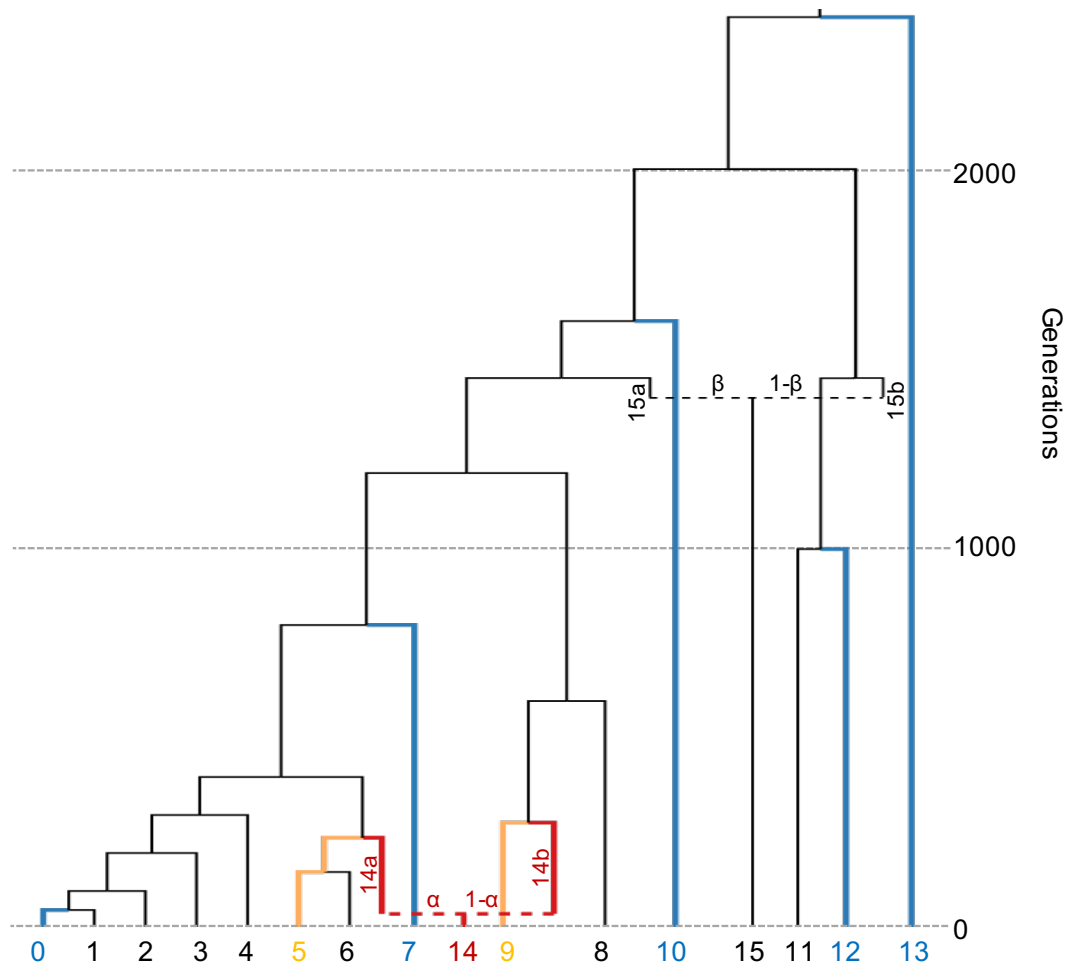
### 166 Data Generation

167 We used msprime version 0.7.1 (KELLEHER *et al.* 2016) to simulate genome-wide data using the  
168 TreeSequence.variants() method, which provides information about all mutations arising in the  
169 dataset and the genotype of individuals at variant sites. We then converted this output to  
170 EIGENSTRAT format (PATTERSON *et al.* 2006). Parameters were chosen in order to mirror what has  
171 been estimated for humans, including a mutation rate of  $1.5 \times 10^{-8}$  mutations per base pair per  
172 generation, recombination rate of  $1.0 \times 10^{-8}$  per base pair per generation, and effective population  
173 sizes between  $2.5 \times 10^4$  and  $8.0 \times 10^5$  (varying between populations and over time; see  
174 Supplementary File 1 for full details). We generated sequence data for 22 chromosomes, each of

175 the approximate length of each of the human autosomes. We simulated  $2 \cdot n$  haploid individuals  
176 then combined pairs of haploid individuals to form  $n$  diploid individuals.

177 In order to assess the performance of qpAdm when the population history of a group is relatively  
178 simple and fully understood, we simulated genetic data according to a base population tree  
179 (Figure 1), consisting of 16 populations and two admixture events (one relatively recent and the  
180 other occurring much earlier in the population history). For the more recent admixture event,  
181 lineages 14a and 14b contribute  $\alpha$  and  $1 - \alpha$  proportion of ancestry to population 14, respectively.  
182 Unless otherwise noted,  $\alpha$  is equal to 0.5. In the earlier admixture event, lineages 15a and 15b  
183 contribute  $\beta$  and  $1 - \beta$  proportion of ancestry to population 15, respectively, where  $\beta$  is equal to  
184 0.55. This tree is an expanded version of a population tree described in PATTERSON *et al.* (2012),  
185 which was used to test the performance of the tool qpGraph. The exact simulation parameters  
186 we used are described in Supplementary File 1. These were chosen so that the overall level of  
187 variation (total number of SNPs) and the differentiation between populations ( $F_{ST}$ ) were similar  
188 to what is observed for humans.

189 For most of our simulations, we generated genomic data for samples taken from 10 (diploid)  
190 individuals from each of the 16 populations in Figure 1. The populations in Figure 1 are idealized,  
191 theoretical populations (see WINTHER *et al.* 2015) and are not meant to represent any particular  
192 human groups. Likewise, the mostly tree-like relationships of populations in Figure 1 simply  
193 reflect the kinds of historical scenarios qpAdm was designed to handle. We consider an example  
194 of non-tree-like structure in the section on continuous gene flow.



**Figure 1. Population history of simulated data.** Populations included in the standard model used for qpAdm models are indicated as follows: target (red), sources (yellow), references (blue).

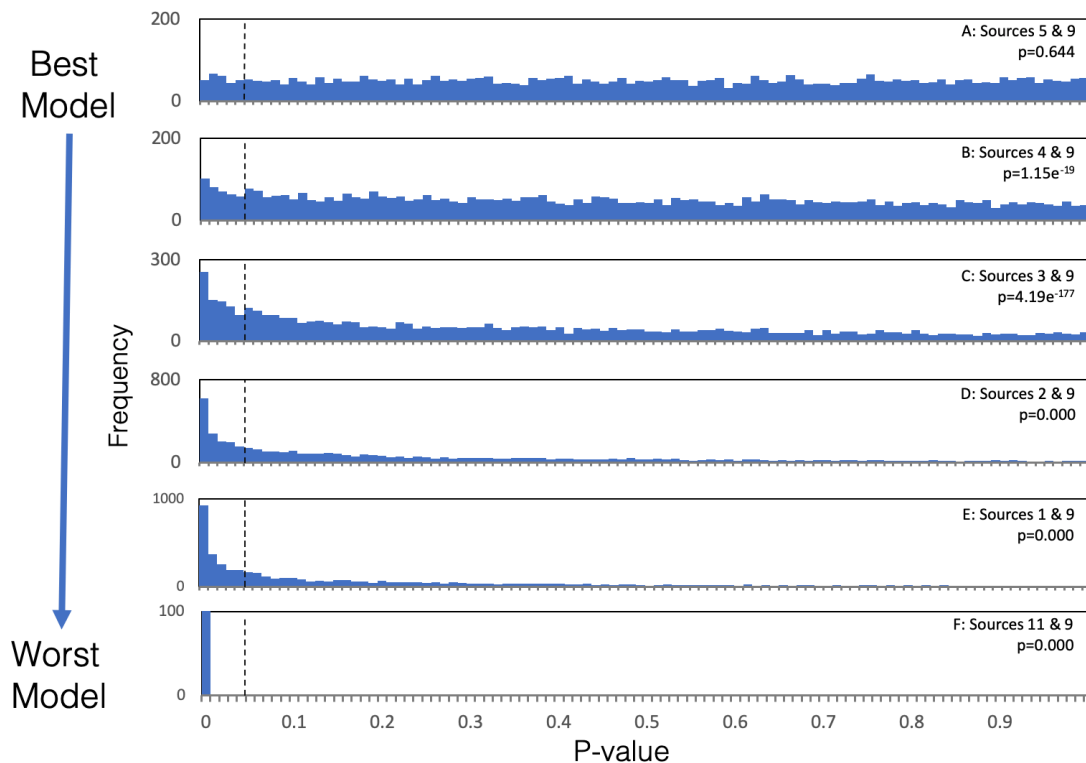
195 Unless otherwise noted, the admixture model of interest is defined as follows; population 14 is  
 196 the target population (the ancestry of which is being modeled), populations 5 and 9 are defined  
 197 as the sources of this admixture, while populations 0, 7, 10, 12, and 13 are designated as  
 198 reference populations. As none of these reference populations are more closely related to the  
 199 target population than to either of the two source populations (i.e. the reference populations do  
 200 not have any shared drift with the target population that is not also shared with at least one of  
 201 the source populations), this model should be considered plausible. This model will be referred  
 202 to as the standard model. Note that because populations 5 and 6 are symmetrically related to

203 population 14, both represent be equally good sources of its ancestry. Unless otherwise noted,  
204 population 6 will therefore be excluded from analyses.

205 All qpAdm analyses were performed using qpAdm version 960, using default parameters, and the  
206 optional parameters, “allsnps: YES”, “details: YES” and “summary: YES”, unless otherwise  
207 specified. See Supplementary Materials 1 for a complete description of all qpAdm parameters.

### 208 [Distribution of p-values](#)

209 qpAdm outputs a p-value that is used to determine whether a specific model of population  
210 history can be considered plausible. Models are rejected, or regarded as implausible, when the  
211 p-value is below the chosen significance cutoff (typically 0.05). In order for true models to be  
212 rejected properly at this nominal significance level, that is only 5% of the time, the distribution  
213 of p-values should be uniform when the null model is equal to the true model. However, this  
214 assumption of uniformity of p-values in qpAdm has never been confirmed. We therefore  
215 assessed the distribution of p-values produced by qpAdm by simulating 5,000 replicates under  
216 our standard model (defined in Figure 1) and running qpAdm on each replicate using the target,  
217 source and reference populations defined in the standard model. We find that the p-values  
218 generated by qpAdm appear uniformly distributed (Figure 2A; Supplementary Table 1). Using a  
219 Kolmogorov-Smirnov test, we fail to reject the null hypothesis that the calculated p-values are  
220 uniformly distributed ( $p=0.644$ ), supporting theoretical predictions for the uniform distribution  
221 of p-values generated by qpAdm when an accurate model is presented.



**Figure 2. Distribution of p-values generated for various qpAdm models.** The distribution of p-values generated by 5,000 replicates of qpAdm is shown for all models, except when sources 11 & 9 are used, in which case only 100 replicates were generated. Panel A shows the distribution of p-values produced by models using populations 5 & 9 as sources, which are the best possible sources of ancestry for population 14 out of the proposed models. Panels B-F show the distribution of p-values produced by models that use increasingly inappropriate source populations, relative to the chosen reference populations. Vertical black dotted lines indicate the p-value threshold of 0.05, above which qpAdm models are considered plausible. The results of a Kolmogorov-Smirnov test to determine whether the p-values are uniformly distributed are indicated.

222 As qpAdm is often used to distinguish between optimal and non-optimal models of admixture,  
 223 we also seek to confirm that the distribution of p-values is not uniform when an incorrect model  
 224 is considered. We therefore examine the distribution of p-values produced when non-optimal  
 225 populations (i.e. populations 1-4 and 11) are used as sources instead of population 5. As  
 226 populations 1-4 share more genetic drift with reference population 0 than the true source  
 227 population (and similarly because population 11 shares less drift with population 0 than the true  
 228 source population), we expect that the distribution of p-values produced by qpAdm should be

229 biased towards zero when these populations are used as sources (with population 11 producing  
230 the strongest bias). We ran these non-optimal qpAdm models on the 5,000 replicate datasets  
231 described above and observe a deviation from a uniform distribution. In the case of populations  
232 1-4, models that include source populations that share the most drift with population 0 yield p-  
233 value distributions that are most strongly biased towards zero (Figure 2B-F; Supplementary Table  
234 1), and as expected, p-values associated with using population 11 as a source are even more  
235 strongly biased towards zero. In each case, using a Kolmogorov-Smirnov test, we reject the null  
236 hypothesis that the p-values are uniformly distributed.

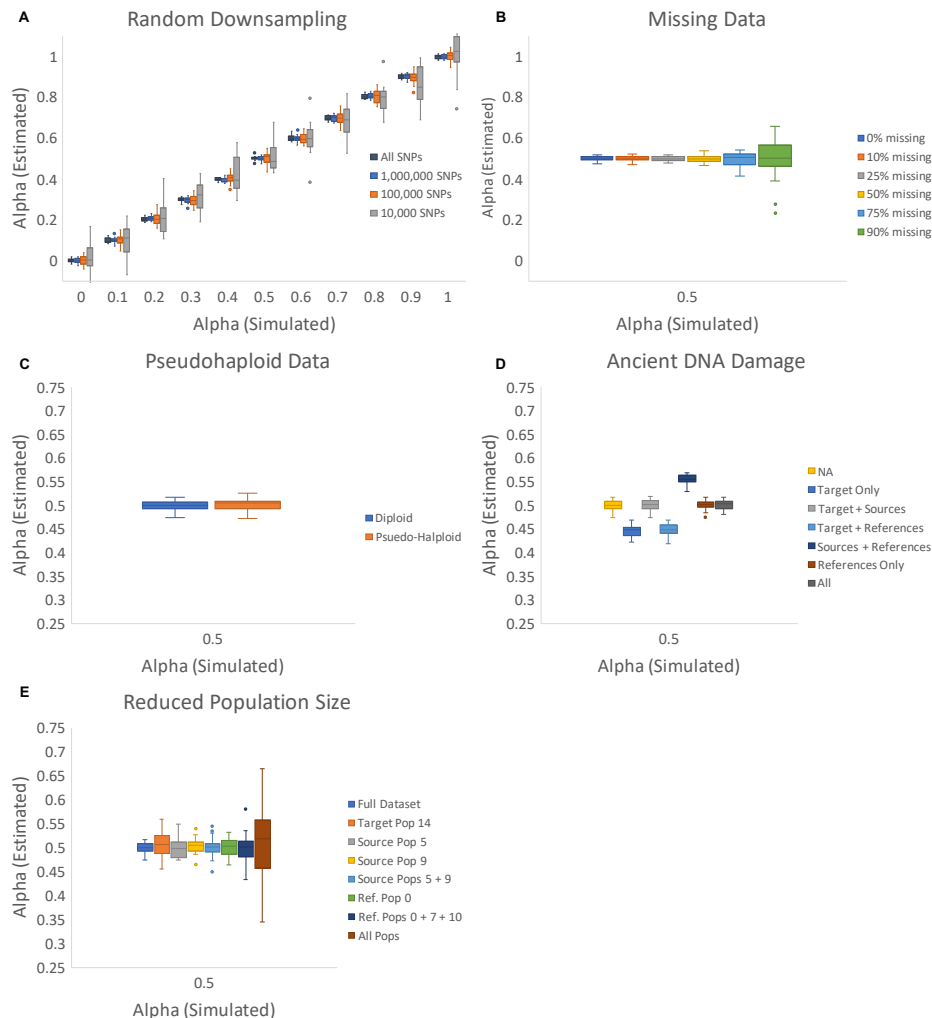
237 Although the distributions of p-values deviate from a uniform distribution as expected, we also  
238 note that in the cases where populations 1-4 are used as potential source populations, a large  
239 proportion of these models are assigned p-values that would be considered plausible using 0.05  
240 as a standard threshold. These results reflect the fact that populations 1-5 are all closely related  
241 (average pairwise  $F_{ST}$  between  $<0.001-0.005$ ), therefore the inclusion of population 0 as the only  
242 reference population with the power to distinguish between these populations (as it is  
243 differentially related to them), may not be enough to reject models that use populations 1-4 as  
244 sources in all cases. In practice, if populations 1-5 were all proposed as potential sources and  
245 qpAdm assigned plausible p-values to multiple models, further analysis would be required to  
246 distinguish between these models. Further, we do note that when population 0 is excluded from  
247 the reference population set, all of the tested qpAdm models using populations 1-5 as a potential  
248 sources, produce approximately uniformly distributed p-values, as would be expected  
249 theoretically, as populations 1-5 are all symmetrically related to all other reference populations  
250 (Supplementary Figure 1; Supplementary Table 2).

251 While the overall distributions of p-values differ between optimal and non-optimal qpAdm  
252 models, we note that for individual replicates the most optimal model is not necessarily assigned  
253 the highest p-value. We find that the p-value associated with the best model (sources 5 & 9)  
254 produces the highest p-value in only 48% of cases (Supplementary Table 1). Therefore, in cases  
255 where multiple models are assigned plausible p-values (i.e.  $p \geq 0.05$ ), we caution that p-value  
256 ranking (i.e. selecting the model that is assigned the highest p-value) should not be used to  
257 identify the best model. Methods for distinguishing between multiple models will be discussed  
258 further in the section on comparing admixture models.

### 259 Accuracy of Admixture Proportion Estimates

260 In addition to generating informative p-values, it is essential that qpAdm generates accurate  
261 admixture proportion estimates. This has also not been formally tested using simulated data. We  
262 therefore simulate genetic data according to the population tree shown in Figure 1, varying the  
263 proportion of admixture ( $\alpha$ ) occurring in the lineage ancestral to population 14 between 0.0-1.0  
264 at intervals of 0.1 with 20 replicates per interval. We find that the estimated admixture  
265 proportions are extremely close to the actual simulated admixture proportions for all values of  $\alpha$   
266 (Figure 3A; Supplementary Table 3). In 99.3% of cases (220 total), the estimated  $\alpha$  is within 3  
267 standard errors of the simulated  $\alpha$ , consistent with theoretical expectations, with an average  
268 standard error of 0.0092 [range: 0.008-0.011]. These results indicate that qpAdm accurately  
269 estimates admixture proportions, regardless of the level of admixture, and that the standard  
270 errors produced by qpAdm are well calibrated. However, we recognize that in practice, users of

271 qpAdm have access to a much less complete dataset. Therefore, we modify the data in order to  
 272 explore the performance of qpAdm when applied to data of lower coverage and quality.



**Figure 3. Accuracy of Admixture Proportion Estimates.** Box and whisker plots showing the estimated values of admixture proportion (alpha) generated by qpAdm for varying simulated alphas. Only alpha 0.5 is shown for panels B-E, however all alphas 0-1 are reported in the corresponding Supplementary Tables. For each simulated alpha, 20 replicates of qpAdm are performed for each condition. [A] Estimates produced by qpAdm when run on the entire dataset and after randomly down-sampling to 1 million, 100 thousand, and 10 thousand SNPs. All subsequent analyses are performed on the 1 million SNP downsampled dataset [B] Estimates produced by qpAdm where some proportion (0%, 10%, 25%, 50%, 75% or 90%) of data is missing in each individual. [C] Estimates produced by qpAdm in both diploid and pseudo-haploid form. [D] Estimates produced by qpAdm where 5% ancient DNA damage is simulated in a subset of populations (14, 14+5+9, 14+0+7+10+12+13, 5+9+0+7+10+12+13, 0+7+10+12+13, and All populations). [E] Estimates produced by qpAdm, where only a single individual is sampled from varying populations (14, 5, 9, 5+9, 0, 0+7+10, and all populations).



273 Each simulation contains an average of ~30 million SNPs. In order to understand the performance  
274 of qpAdm with less data, we randomly down-sample the complete dataset to produce analysis  
275 datasets of 1 million, 100 thousand, and 10 thousand sites. In all cases, the average admixture  
276 proportion estimate generated is extremely close to the simulated  $\alpha$ , although we do observe an  
277 increase in the amount of variance in the individual estimates as the amount of data analyzed  
278 decreases (Figure 3A; Supplementary Table 3). In order to increase computational efficiency and  
279 to better approximate typical analysis datasets, all subsequent analyses are performed on the  
280 data that has been randomly down-sampled to 1 million sites. We observe similar results when  
281 using non-random ascertainment schemes to select sites for analysis (Supplementary Table 4).  
282 The impact of non-random ascertainment schemes on qpAdm analyses are described in more  
283 detail in a later section.

284 We find that qpAdm is robust to missing data, where data from randomly selected sites in each  
285 individual is considered missing with rate 10%, 25%, 50%, 75% or 90% (Figure 3B; Supplementary  
286 Table 5). Additionally, we find that pseudohaploidy—a common feature of ancient DNA, where  
287 due to low sequencing coverage, a haploid genotype is determined by randomly selecting one  
288 allele at each diploid site and assigning that to be the genotype—has little impact on admixture  
289 estimates (Figure 3C; Supplementary Table 6).

290 Ancient DNA is also subject to deamination, resulting in C-to-T or G-to-A substitutions appearing  
291 in transition sites. In the 1.2 million SNP sites that are commonly targeted in ancient DNA analysis,  
292 approximately 77.6% of sites are transitions (FU *et al.* 2015; HAAK *et al.* 2015; MATHIESON *et al.*  
293 2015). We therefore randomly defined 77.6% of simulated sites to function as transitions. For

294 each of these transition sites, in each individual, if the allele at that position is of the reference  
295 type, it was changed to the alternative type with 5% probability, mimicking the unidirectional  
296 change in allelic state caused by ancient DNA damage. We find that admixture proportion  
297 estimates produced by qpAdm are relatively robust to the presence of ancient DNA damage in  
298 cases where all populations exhibit an equal damage rate (Figure 3D; Supplementary Table 7).  
299 However, in cases where the target (population 14) and source (5 + 9) populations have a  
300 different rate of ancient damage the estimated admixture proportions are biased. This bias  
301 reflects attraction between populations on the left and right sides of the  $f_4$ -statistics calculated  
302 by qpAdm and is not unexpected. The effects of differential rates of ancient DNA damage  
303 between populations on qpAdm analyses are explored further in a later section.

304 Another concern that is common among ancient DNA analyses is small sample size. We therefore  
305 explore the effect of reducing the sample size of various populations in the analysis from ten  
306 individuals down to a single individual. We find that admixture estimates are relatively robust to  
307 this reduced sample size regardless of whether the target (population 14), source (population 5,  
308 9, or 5 + 9) or reference (population 0 or 0 + 7 + 10) set has only a single individual sampled  
309 (Figure 3E; Supplementary Table 8). Reducing the target sample size to a single individual appears  
310 to have the greatest effect for all cases where only the sample size of a single population was  
311 reduced. Further, we see that when only a single individual is sampled from every population,  
312 the admixture proportion estimates vary the most between replicates, however, the mean of  
313 these estimates fall close to the true  $\alpha$ , suggesting that small sample size does not result in an  
314 upward or downward bias in the admixture proportion estimates produced by qpAdm.

315 While none of the factors considered here result in biased admixture proportion estimates  
316 (except for when ancient DNA damage is present non-uniformly across populations), we caution  
317 that the increase in variance associated with each of these forms of reduced data quality is likely  
318 to be additive, so models relying on data with high rates of missingness, damage and very small  
319 sample sizes should be interpreted with caution.

## 320 [Comparing Admixture Models](#)

321 One of the major applications of qpAdm is to identify an optimal admixture model, out of a  
322 variety of proposed possible models, many of which may be deemed plausible by qpAdm.  
323 However, no formal recommendations have been made about what strategy to use when  
324 comparing models. We therefore explore two commonly employed approaches for comparing  
325 admixture models in order to make recommendations for best practices in qpAdm usage.

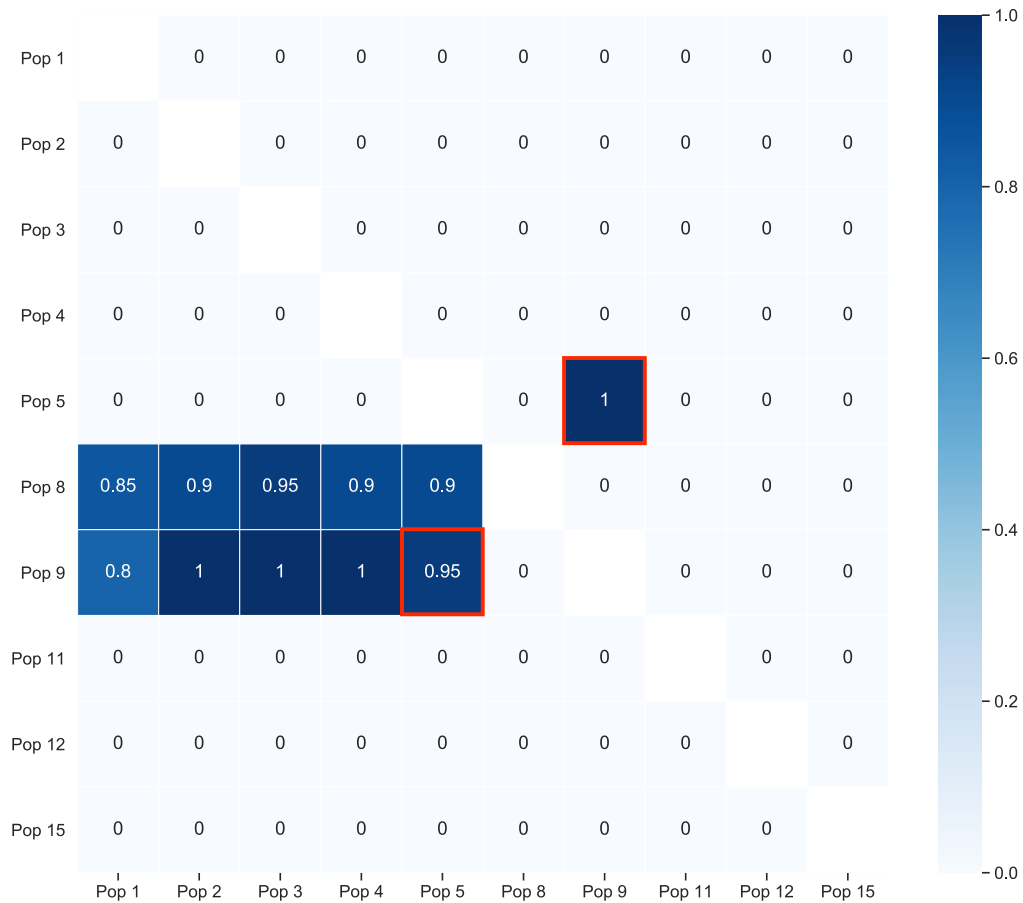
326 One of the most typical implementations of qpAdm involves the selection of a set of differentially  
327 related populations to serve as the base set of reference populations. This base set of reference  
328 populations is often chosen to represent key positions in the known population history (i.e. the  
329 'O9' reference set defined in LAZARIDIS *et al.* (2016)). A non-overlapping set of source populations  
330 is then defined, and qpAdm models involving different combinations of source populations and  
331 the base set of reference populations are tested. Using this method, multiple models may meet  
332 the criteria to be considered plausible, and the most optimal model is identified by adding  
333 additional reference populations to the base set of references, which are selected for their  
334 differential relatedness to one or more of the source populations in the set of potentially  
335 plausible qpAdm models.

336 While this strategy is relatively straightforward and widely implemented (e.g. LAZARIDIS *et al.*  
337 2016; HARNEY *et al.* 2018), it has several drawbacks. In particular, because a population cannot  
338 simultaneously serve as a source and reference population, this strategy either requires that  
339 populations that are placed in the base set of reference populations are not considered as  
340 potential source populations (meaning it is possible that the best source population would be  
341 entirely missed if it were selected to serve in the reference population set) or that potential  
342 source populations be selectively removed from the reference population set so that they can be  
343 used as source populations for some models. This strategy results in the creation of some models  
344 that are not equivalent, and therefore are difficult to compare.

345 An alternative to the “base” reference set strategy that has been implemented in order to avoid  
346 these problems is to create a set of “rotating” models in which a single set of populations is  
347 selected for analysis (e.g. SKOGLUND *et al.* 2017; HARNEY *et al.* 2019). From this single set of  
348 populations, a defined number of source populations are selected, and all other populations then  
349 serve in the reference population set for the model. Under this “rotating” scheme, populations  
350 are systematically moved from the set of reference populations to the set of sources. Thus, all  
351 population models are generated using a common set of principles and are therefore more easily  
352 directly compared. In order to compare the performance of these two strategies (“base” versus  
353 “rotating”), we again focus on the population history of population 14 (Figure 1).

354 For the “base” reference approach, we continue to use the base set of reference populations as  
355 previously defined (populations 0, 7, 10, 12, and 13), all other populations are considered to be  
356 potential source populations. We used qpAdm to test all possible combinations of two source

357 populations. We ran each of these qpAdm models on the data generated using the standard  
358 population history with  $\alpha=0.50$ , with 20 replicates. Among these 20 replicates, qpAdm identified  
359 the optimal model, in which populations 5 and 9 serve as source populations, as plausible in 19  
360 cases (Figure 4; Supplementary Table 9). However, there are also a large number of other  
361 population models that are consistently deemed plausible; for example when population 8 is  
362 used as a source (in conjunction with population 5) instead of population 9, 90% of the models  
363 are deemed plausible. The high rate of acceptance of this model is fully consistent with  
364 expectations, because while population 9 is more closely related to the true source population,  
365 populations 8 and 9 are symmetrically related to all of the reference populations included in the  
366 model, and therefore are indistinguishable using this approach (unless data from a population  
367 that differentially related to these two populations could be added to the model). Models that  
368 include populations 1-4 (in combination with populations 8 or 9) were also frequently identified  
369 as plausible. These results suggest that the inclusion of population 0 as a reference does not  
370 provide enough information to differentiate between these potential source populations and the  
371 true optimal source (population 5). Therefore, the next step in a qpAdm analysis that utilizes the  
372 base model approach would be to add additional reference populations that are differentially  
373 related to populations 1-5 in order to help differentiate between the remaining possible models.



**Figure 4. Comparing qpAdm models using various approaches.** A heatmap showing the proportion replicates in which the 2-way admixture model generated using each combination of possible source populations is deemed plausible by qpAdm (i.e. yielded a p-value > 0.05 and admixture proportion estimates between 0-1). The lower triangle shows results generated using the base set of reference populations (0, 7, 10, 12, and 13), while the upper triangle shows results generated the rotating model approach. The proportion of replicates deemed plausible is indicated by the color (darker shades indicate a higher proportion) and is written inside each square of the heatmap. The optimal admixture model(s) for each of the approaches are highlighted in red.

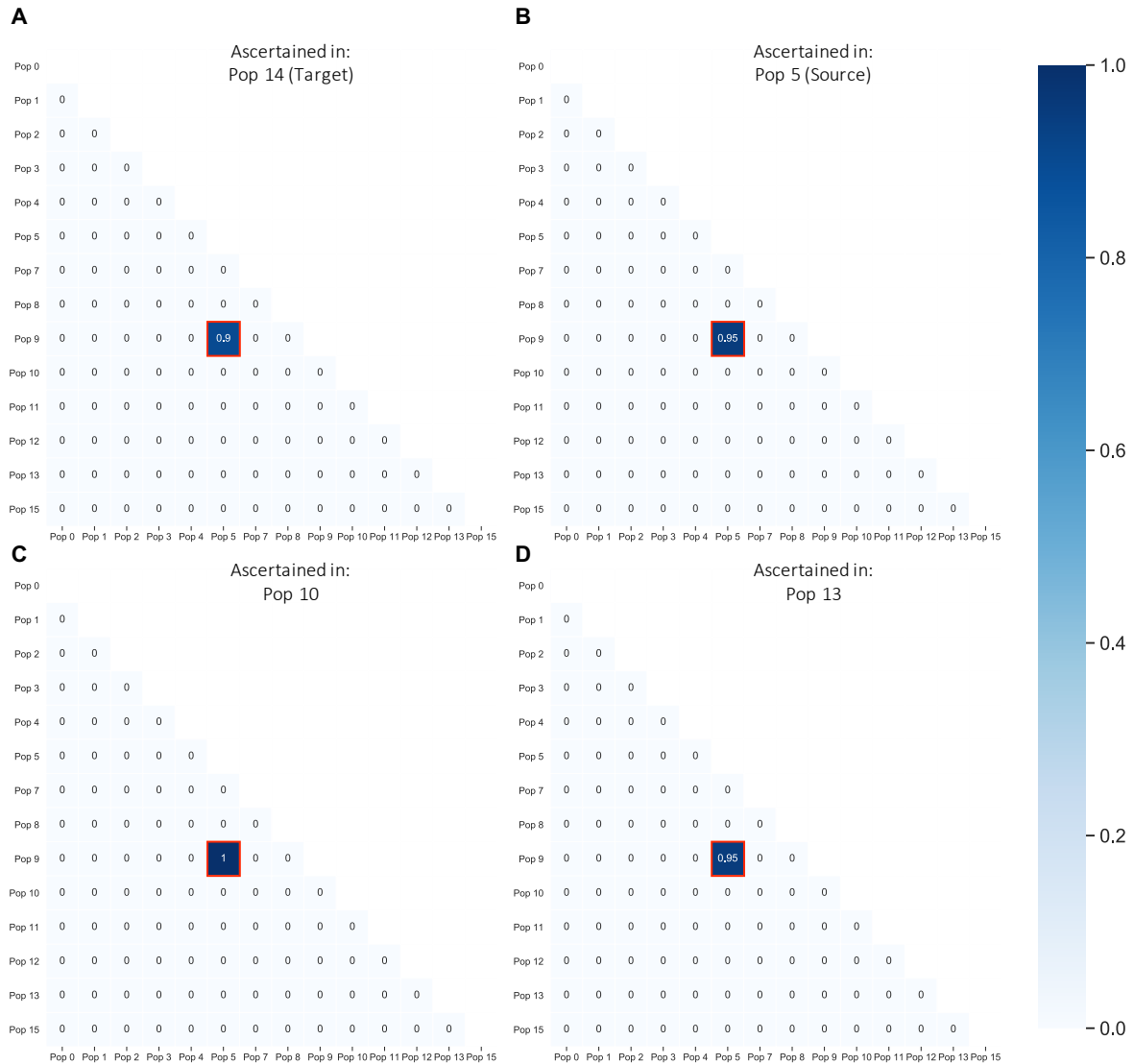
374 In contrast, we find that under a “rotating” model, where all populations (except for population  
 375 6 because it is phylogenetically a clade with source 5) were selected to serve as either a source  
 376 or a reference population, all models that included populations 5 and 9 as sources were identified  
 377 as plausible. In contrast all other population models were rejected (Figure 4; Supplementary  
 378 Table 10). The inclusion of the optimal source populations (5 & 9) as references in all other  
 379 models enables qpAdm to differentiate between models that would otherwise be

380 indistinguishable (such as differentiating between populations 8 and 9 and between populations  
381 1-5). Further, in cases where optimal source populations are not available (i.e. if both populations  
382 5 and 6 are excluded from the model), qpAdm still identifies closely related models as plausible  
383 (such as those involving admixture between population 9 and populations 0-4), suggesting that  
384 this rotating approach is not overly stringent in cases where optimal data are not available  
385 (Supplementary Table 11). Due to the relative simplicity of the rotating model approach and the  
386 increased ability to identify the optimal admixture model when using it, we recommend utilizing  
387 a rotating strategy when possible.

#### 388 *Ascertainment bias and “rotating” model selection*

389 In order to understand the impact of ascertainment bias on model selection, we repeated this  
390 analysis on data that was ascertained from the full dataset using several non-random  
391 ascertainment strategies, including ascertaining on sites that were found to be heterozygous in  
392 a single individual from [1] the target (population 14), [2] a source (population 5), and [3] two  
393 populations that are uninvolved in the admixture event (population 10 and 13). The individual  
394 used for data ascertainment was excluded from subsequent analyses. In all cases, using the  
395 rotating approach previously described, only models that use populations 5 and 9 as sources are  
396 deemed plausible (Figure 5; Supplementary Table 12), suggesting that ascertainment bias is  
397 unlikely to cause users to identify inappropriate models as plausible. Further, the optimal model  
398 was identified as plausible in at least 90% of replicates using all ascertainment strategies,  
399 suggesting that qpAdm is robust to ascertainment bias. These results are consistent with previous

400 findings that  $f_4$ -statistics, which are used for all qpAdm calculations, are robust to biased  
 401 ascertainment processes (PATTERSON *et al.* 2012).



**Figure 5. Effect of ascertainment bias on qpAdm model selection.** Heatmaps showing the proportion of replicates in which the 2-way admixture model generated using each combination of possible source populations is deemed plausible by qpAdm (i.e. yielded a p-value > 0.05 and admixture proportion estimates between 0-1) on SNP data that is ascertained from a heterozygous individual in a single population, [A] population 14 (target), [B] population 5 (source), [C] population 10 and [D] population 13. The proportion of replicates deemed plausible is indicated by the color (darker shades indicate a higher proportion) and is written inside each square of the heatmap. The optimal admixture model for each of the approaches are highlighted in red.



402 *Missing data and the “allsnps” option of qpAdm*

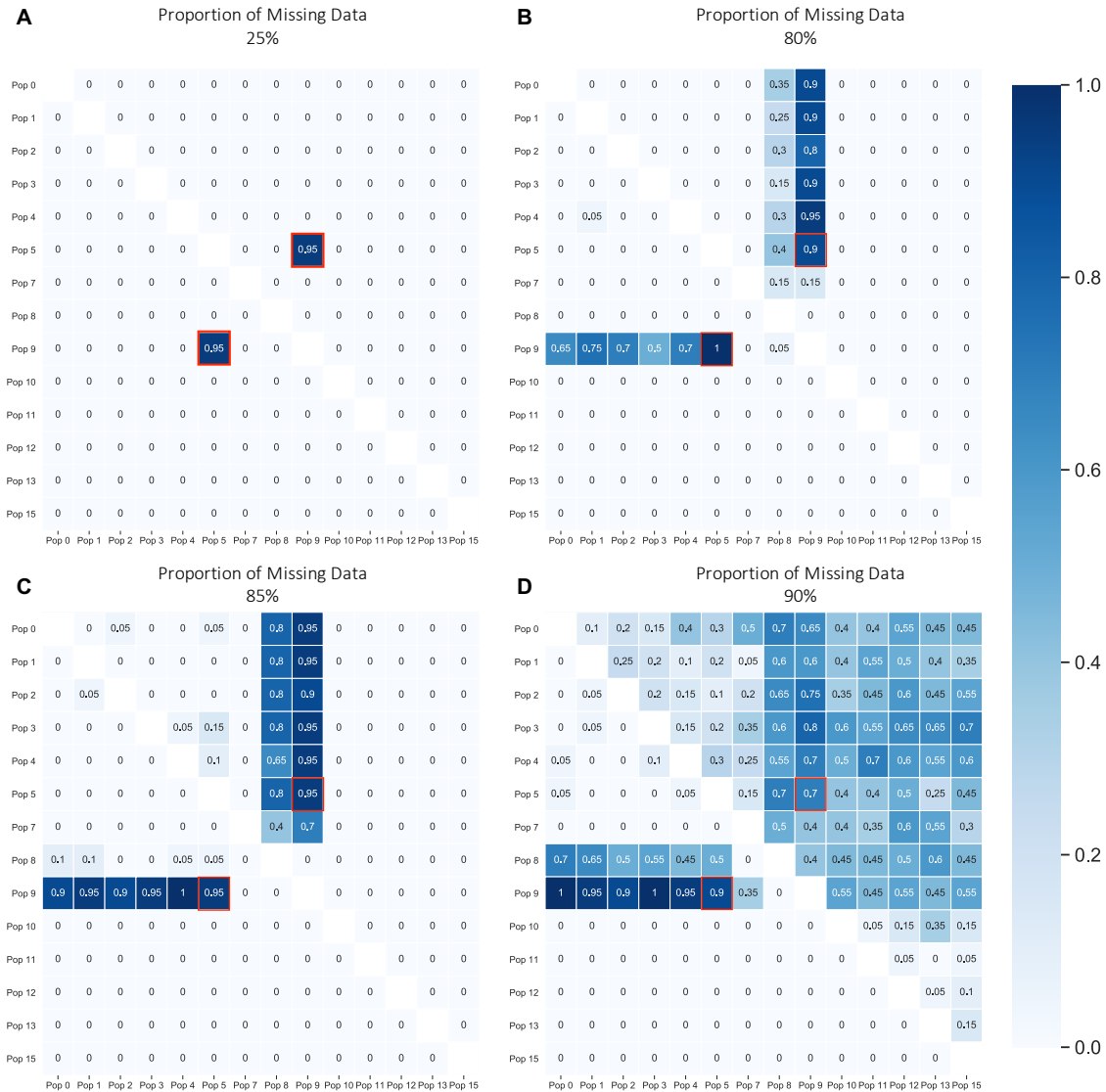
403 We also explored the effect of qpAdm’s “allsnps” option when working with samples with a large  
404 amount of missing data. If the default “allsnps: NO” option is selected, qpAdm only analyzes sites  
405 that are shared between all target, source, and reference populations that are included in the  
406 model. In contrast, if “allsnps: YES” is selected, every individual  $f_4$ -statistic is calculated using the  
407 intersection of SNPs that have available data for the four populations that are involved in that  
408 particular calculation, therefore every  $f_4$ -statistic is calculated using a unique set of sites. The  
409 “allsnps: YES” parameter is commonly used in cases where one or more populations in the  
410 analysis dataset has a high rate of missing data, in order to increase the number of sites analyzed.  
411 However, this causes the underlying calculations performed by qpAdm to deviate from those on  
412 which the theory is based, and the effect of this change in calculations on admixture proportions  
413 estimated by qpAdm and on optimal model identification is not well studied.

414 We explore the effects of this parameter, using simulated data with admixture proportion  $\alpha$   
415 =0.50 and rates of missing data equal to either 25%, 80%, 85% or 90% for all individuals across 1  
416 million SNP sites. We implemented the rotating model for both the “allsnps: YES” and “allsnps:  
417 NO” options (all previous analyses used the “allsnps: YES” option). Comparing all possible models  
418 using the rotating approach, we find that the results produced when using the “allsnps: YES” and  
419 “allsnps: NO” options are similar when the rate of missing data is low (i.e. 25%) (Figure 6A;  
420 Supplementary Table 13). The optimal model (with sources 5 and 9) was identified as plausible  
421 in 95% of cases and no other models were deemed plausible for both options. Further, the  
422 admixture proportion estimates produced in both cases are relatively similar, with average

423 standard errors of 0.006 in both cases. The similar performance of the “allsnps: YES” and  
424 “allsnps:NO” options in this case is likely due to the relatively large sample size (10 individuals  
425 per population) used in the analysis. With 25% missing data, the expected number of SNPs to be  
426 included in the analysis when the “allsnps: YES” option is selected is 1 million. This number is only  
427 slightly reduced, to 999,985.7, when the “allsnps: NO” option is selected.

428 In contrast, when the rate of missing data is elevated (i.e. 80%, 85% or 90%), a difference in  
429 performance between the “allsnps: YES” and “allsnps: NO” options was observed. In each case,  
430 when the rate of missing data increased, the number of non-optimal models that were identified  
431 as plausible also increased (Figure 6B-D). These changes were more dramatic when the “allsnps:  
432 NO” parameter was used, further we observe a greater increase in the standard errors associated  
433 with admixture proportion estimates produced when using the “allsnps: NO” option, with  
434 average standard errors equal to 0.025, 0.066, and 9.994 when analyzing data with 80%, 85%,  
435 and 90% missing data, respectively. In contrast, while the standard errors produced using the  
436 “allsnps: YES” option also increased, the increase was lower in magnitude in all cases, with  
437 standard errors of 0.015, 0.020, and 0.035 observed, respectively. This difference in performance  
438 is likely the result of the number of SNPs available for analysis when using each option. When  
439 using the “allsnps: YES” parameter, the expected number of SNPs used in analysis of data with  
440 80%, 85%, and 90% missing data rates remains 1 million. However, when using the “allsnps: NO”  
441 parameter, the expected number of SNPs used in analysis with each rate of missing data is only  
442 181,987.5, 37,303.7, and 1,610.4 SNPs, respectively. These results suggest that the increased  
443 data provided by using the “allsnps: YES” option improves the ability of qpAdm to distinguish

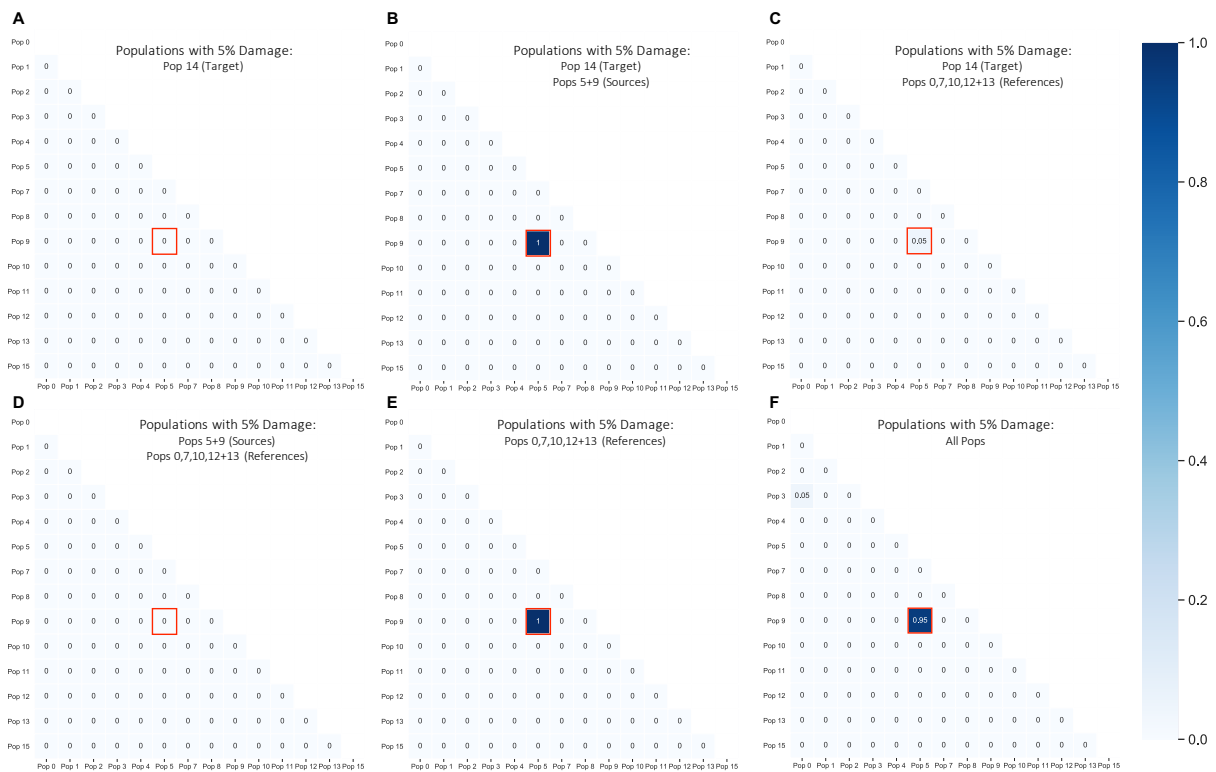
444 between models, without creating biases in cases where missing data is distributed randomly  
 445 throughout the genome of all individuals.



**Figure 6. Effect of the allsnps parameter on qpAdm model selection.** Heatmaps showing the proportion of replicates in which the 2-way admixture model generated using each combination of possible source populations is deemed plausible by qpAdm (i.e. yielded a p-value > 0.05 and admixture proportion estimates between 0-1) on SNP data using the “allsnps: yes” (lower left triangle) and “allsnps: no” parameters (upper right triangle), on data with [A] 25% [B] 80% [C] 85% or [D] 90% missing data. The proportion of replicates deemed plausible is indicated by the color (darker shades indicate a higher proportion) and is written inside each square of the heatmap. The optimal admixture model for each of the approaches are highlighted in red.

446 *The effects of ancient DNA damage on model selection*

447 In an earlier section, we show that admixture proportion estimates produced by qpAdm can be  
 448 biased when produced using populations with differential rates of ancient DNA damage. We  
 449 therefore explored the effects of damage on model comparison, using the rotating model  
 450 approach. Across all cases, only models involving the optimal sources (populations 5 and 9) are  
 451 deemed plausible, suggesting that ancient DNA damage, even when unevenly distributed, is  
 452 unlikely to cause a user to identify a non-optimal model as plausible (Figure 7; Supplementary  
 453 Table 14). Further, when damage rates are consistent between the target and optimal source



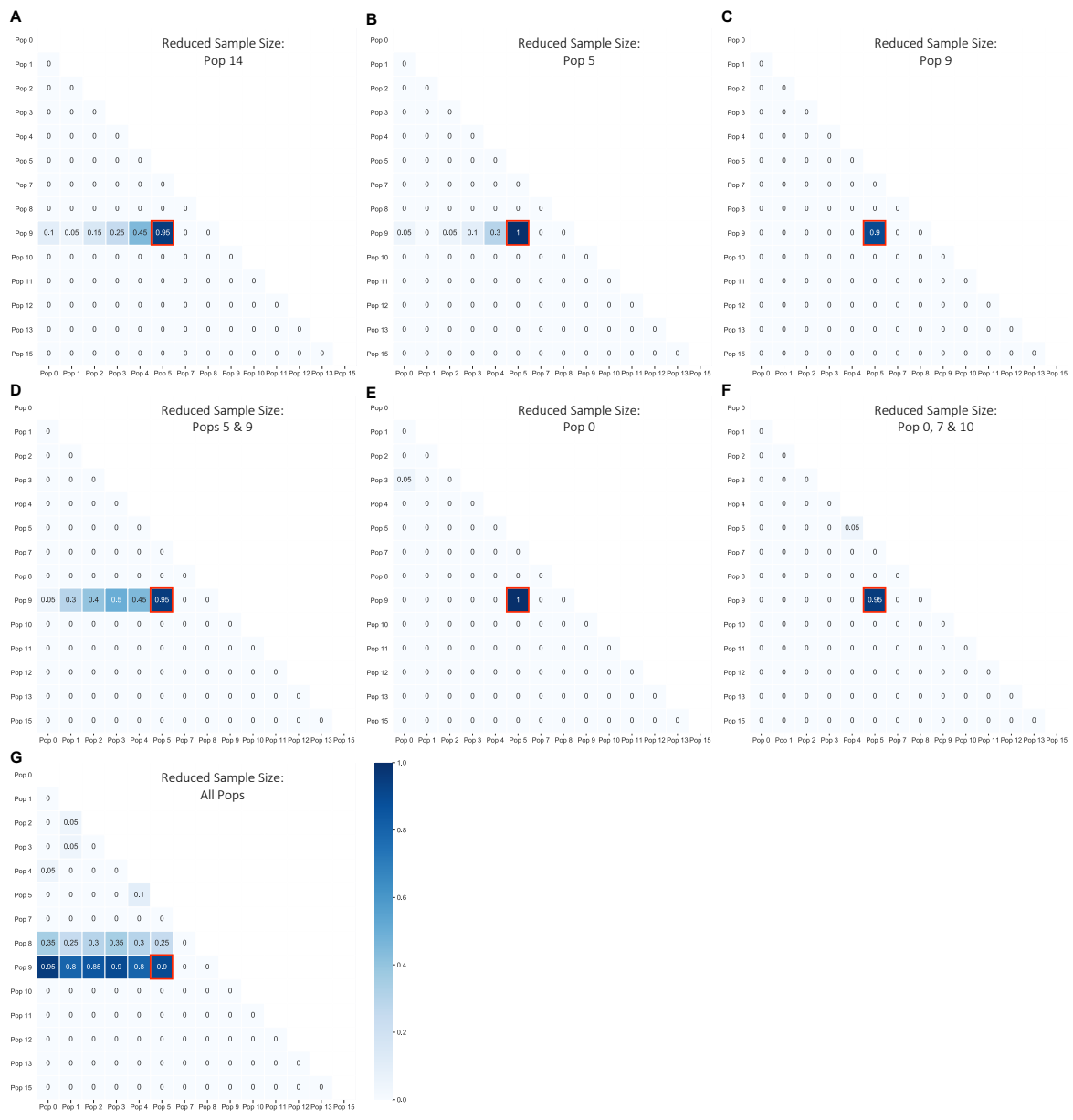
**Figure 7. Effect of ancient DNA damage on model selection.** Heatmaps showing the proportion of replicates in which the 2-way admixture model generated using each combination of possible source populations is deemed plausible by qpAdm (i.e. yielded a p-value > 0.05 and admixture proportion estimates between 0-1) on SNP data. In each case [A-F] a given population or set of populations (14, 14+5+9, 14+0+7+10+12+13, 5+9+0+7+10+12+13, 0+7+10+12+13 and all populations) contain ancient DNA damage at 5% of “transition” sites. The proportion of replicates deemed plausible is indicated by the color (darker shades indicate a higher proportion) and is written inside each square of the heatmap. The optimal admixture model for each of the approaches is highlighted in red.

454 populations, the optimal model is identified as plausible in at least 95% of cases. However, when  
455 the target and source populations have differential rates of damage, this optimal model is almost  
456 always deemed implausible. We do note that the ancient DNA damage simulated in this analysis  
457 (5% ancient DNA damage rate at all “transition” sites) is relatively high, as most ancient DNA  
458 damage occurs at the terminal ends of DNA molecules. Therefore, these results likely represent  
459 an extreme case. However, these results highlight the importance of considering the effect of  
460 ancient DNA damage in ancient DNA analyses. In particular, we caution against designs where  
461 both ancient and present-day populations are included in a single qpAdm model.

#### 462 *The effects of sample size on model selection*

463 We also considered the impact of limited sample size when comparing models, using a rotating  
464 model approach. Using the same data shown in Figure 3E, where the sample size of the specified  
465 population(s) was reduced to 1 (Figure 8; Supplementary Table 15). In cases where the  
466 population(s) with reduced sample size were not involved in the admixture event of interest the  
467 effect of sample size reduction is minimal. Similarly, the results do not appear to be significantly  
468 affected when population 9 (one of the optimal source populations) experiences reduced sample  
469 size, suggesting that when the optimal source population is relatively differentiated from all other  
470 populations considered, reduced sample size has little effect. However, when source population  
471 5 only contained a single sampled individual, models using closely related populations as sources  
472 were also deemed plausible. Similarly, when the target population (14) contained only a single  
473 sampled individual, the proportion of non-optimal models that were identified as plausible by  
474 qpAdm increased. These results suggest that when the sample size is lower, particularly for target  
475 or source populations, qpAdm has less power to reject non-optimal models. This is likely to

476 become an even greater issue in cases where populations included in qpAdm models contain  
 477 only a single individual with large amounts of missing data.



**Figure 8. Effect of reduced sample size on model selection.** Heatmaps showing the proportion of replicates in which the 2-way admixture model generated using each combination of possible source populations is deemed plausible by qpAdm (i.e. yielded a p-value > 0.05 and admixture proportion estimates between 0-1) on SNP data. In each case [A-G] a given population or set of populations (14, 5, 9, 5+9, 0, 0+7+10, and all populations) contain only a single sampled individual. The proportion of replicates deemed plausible is indicated by the color (darker shades indicate a higher proportion) and is written inside each square of the heatmap. The optimal admixture model for each of the approaches is highlighted in red.

478 *Modeling unadmixed populations using qpAdm*

479 Finally, while we know that the population history of population 14 involves admixture, the  
480 number of ancestral sources that contributed ancestry to a real target population is typically  
481 unknown. Therefore, we explored the behavior of qpAdm when modeling the population history  
482 of unadmixed and admixed populations (populations 6 and 14, respectively) under various  
483 scenarios. First, we explored models in which only a single source population contributed  
484 ancestry to the target population, using the same rotating model as described previously, but  
485 only selecting a single source population for each model. In the case of the unadmixed population  
486 6, we find that in 95% of cases, it can be modeled as forming a genetic clade with population 5,  
487 consistent with theoretical expectations (Supplementary Table 16). In contrast, population 14 is  
488 never found to form a genetic clade with any of the tested source populations (Supplementary  
489 Table 17), again consistent with expectations. However, when population 6 is modeled as the  
490 product of admixture between 2 source populations, we find that it is frequently modeled as the  
491 product of a two-way admixture between population 5 and any other source population, where  
492 population 5 is estimated to contribute the vast majority of ancestry to population 6  
493 (Supplementary Table 18)—in cases where these models are rejected, it is typically because  
494 population 5 is modeled as contributing greater than 100% of the ancestry to population 6, rather  
495 than due to a low p-value. We therefore stress the importance of testing all possible models with  
496 the lowest rank (i.e. number of source populations) using qpAdm (or the related qpWave) before  
497 proceeding to test models with higher rank.

## 498 Challenging Scenarios

499 While we find that qpAdm behaves as expected under standard conditions, we are also  
500 interested in identifying scenarios under which qpAdm might behave in unanticipated and  
501 undesirable ways. We therefore explore the performance of qpAdm under two challenging  
502 scenarios: when the number of reference populations is very large and when the relatedness of  
503 populations is not tree-like but rather reflects ongoing genetic exchange.

### 504 *Number of reference populations*

505 We were interested in the effect of assigning an extremely large number of populations to the  
506 reference population set. While a commonly employed method for distinguishing between  
507 optimal and non-optimal admixture models and reducing the standard errors associated with a  
508 admixture proportion estimates is to increase the number of reference populations included in  
509 qpAdm models (e.g. LAZARIDIS *et al.* 2016; HARNEY *et al.* 2018), the effect of including too many  
510 reference populations in a model is unknown. As qpAdm generates  $f_4$ -statistics involving  
511 combinations of reference populations, the larger the number of reference populations is, the  
512 more poorly estimated the covariance matrix of these  $f_4$ -statistics is predicted to be. Therefore,  
513 existing guidelines for qpAdm usage recommend against assigning too many populations to the  
514 reference set, as the computed p-values are thought to be unreliable. However, how many  
515 reference populations is “too many” and what the effect of exceeding this number would be on  
516 the calculated p-values is unknown.

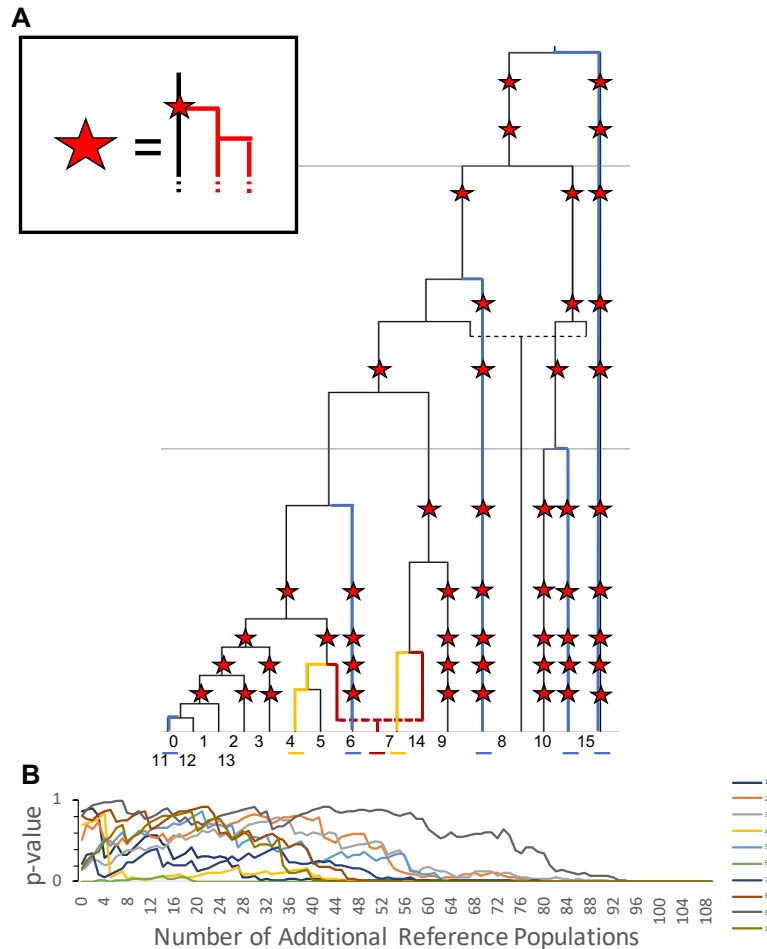


517 We therefore simulated a dataset with a large number of populations by adding two additional  
518 population branching events, occurring 50 generations apart, to all locations on the standard  
519 population tree that are marked with a star in Figure 9A, resulting in a total of 118 total  
520 populations in the simulated dataset (see Supplementary File 2 for exact simulation parameters).  
521 After down-sampling the simulated data to 1 million sites, we then ran qpAdm, with population  
522 14 as the target, and populations 5 and 9 as sources. Populations 0, 7, 10, 12 and 13 were again  
523 assigned to serve as reference populations. All other populations (excluding population 6) were  
524 added, one at a time in random order to the reference population set, resulting in qpAdm models  
525 with between 5 and 114 reference populations. As each new reference population was added to  
526 the model, we re-ran qpAdm and recorded the p-value.

527 Figure 9B shows the change in estimated p-value as reference populations are added to the  
528 model for 10 separate replicates (Supplementary Table 19). While the p-values calculated for  
529 each replicate using the original set of 5 reference populations appear to fall randomly between  
530 0-1 (consistent with the uniform distribution of p-values observed in earlier analyses), we find  
531 that in all cases, as the number of reference populations increases the p-values eventually fall  
532 below the threshold of 0.05, resulting in all of the models with the maximum number of reference  
533 populations to be rejected. These results indicate that the inclusion of too many reference  
534 populations is likely to result in the rejection of qpAdm models, even in cases where the optimal  
535 source populations have been specified.

536 The maximum number of reference populations that can be included in a qpAdm model before  
537 this effect is observed is likely to depend on the specific population history and the total amount

538 of data included in the analysis. In these simulations, we find that qpAdm begins to reject models  
 539 that would otherwise be deemed plausible when as few as 30 additional populations are added  
 540 to the outgroup set. These results support previous warnings against including too many  
 541 reference populations in qpAdm models.

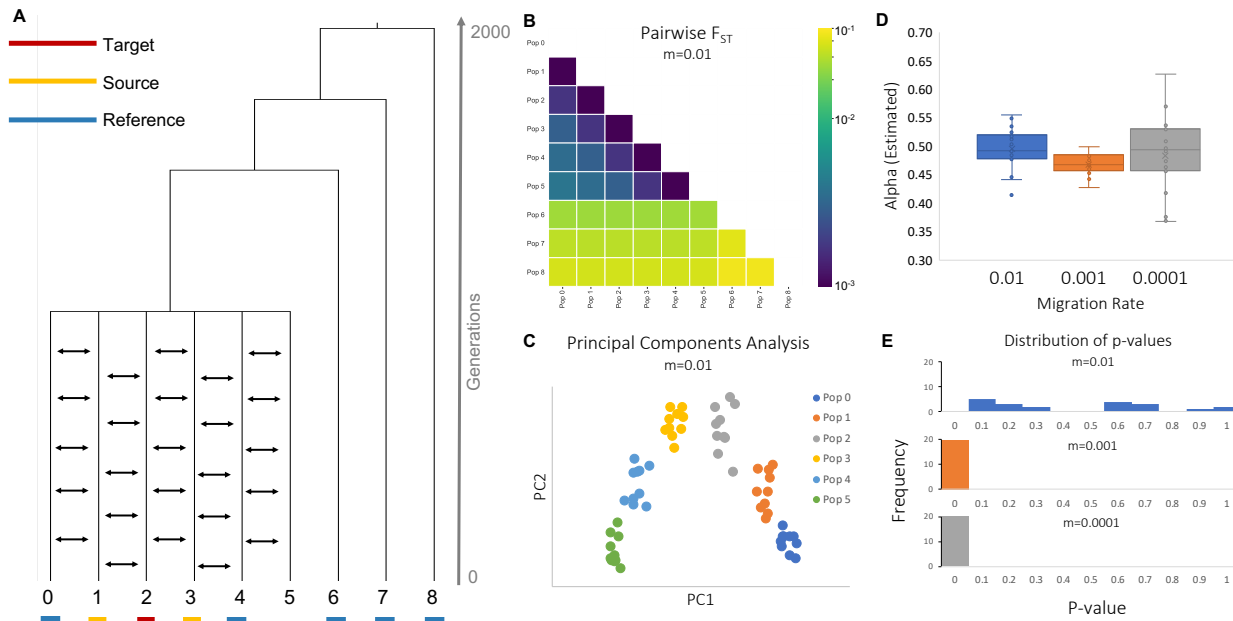


**Figure 9. Inclusion of a large number of reference populations.** (A) Population history of simulated data with additional populations added to tree. In all positions in the population history marked by a star, a population branching event occurs, forming an additional population. This new lineage undergoes an additional population branching event 50 generations later, resulting in two new populations created at each location marked with a star. Colors indicate the populations used in the base model, with the target in red, sources in yellow, and initial references shown in blue. (B) The change in p-values assigned to each model by qpAdm as additional reference populations are randomly added to the model. Each line tracks the p-values assigned to a single replicate, as the number of additional reference populations added to the base set of reference populations increases from 0 to 100.

542 *Continuous gene flow*

543 An underlying assumption of qpAdm is that population admixture occurs in a single pulse over a  
544 small interval of time, during which the proportion of ancestry coming from each of the ancestral  
545 source populations can be estimated. However, real population histories often involve  
546 continuous gene flow that occurs over a prolonged period of time. In this case, although the  
547 resulting population may have received ancestry from multiple sources, estimates of admixture  
548 proportions from these sources may not be meaningful.

549 We therefore consider data simulated using a stepping-stone model of migration, in which  
550 neighboring populations exchange migrants each generation with rate,  $m$  (KIMURA AND WEISS  
551 1964). We simulated a population history based on this migration model (Figure 10A), where 6  
552 populations (each with an effective population size of 10,000) split from a common ancestral  
553 population 1000 generations previously, after which point migration occurred between  
554 neighboring populations. The model also includes three additional populations that are  
555 symmetrically related to these 6 populations, with all 9 lineages splitting from a common  
556 ancestral population 2000 generations in the past (see Supplementary File 3 for exact simulation  
557 parameters).



**Figure 10. Continuous migration models.** (A) Population history involving continuous migration. The target, source, and reference populations underlined in red, yellow, and blue, respectively. (B) A heatmap showing average pairwise  $F_{ST}$  between each population for 20 replicates (C) A PCA plot showing the relationship between all populations, calculated using a single replicate (D) Admixture proportions assigned by qpAdm for a model with population 2 as the target, and populations 1 and 3 as sources at varying migration rates. (E) Histograms showing the frequency of p-values produced by this qpAdm model at varying migration rates.

558 While under this model, populations 1 and 3 have each contributed ancestry to population 2, it  
 559 would be inaccurate to say that population 2 is the product of admixture between these two  
 560 populations. The duration of exchange of ancestry is much longer than what is supposed in  
 561 qpAdm. In addition, population 2 was formed in the same population-splitting event that formed  
 562 populations 1 and 3, not as the result of admixture between distinct populations 1 and 3. Finally,  
 563 by symmetry population 2 is just as much the source of populations 1 and 3 as either of these is  
 564 the source of population 2.

565 Preliminary analyses of the relationships between these 9 populations using pairwise  $F_{ST}$   
 566 (PATTERSON *et al.* 2006) would indicate that population 2 is closely related to both populations 1

567 and 3 (Figure 10B; Supplementary Table 20). Further, if populations 0-5 are plotted using PCA  
568 (Figure 10C; Supplementary Table 21)(PATTERSON *et al.* 2006), population 2 appears to fall on a  
569 genetic cline between these two populations. These results could be interpreted as suggestions  
570 that population 2 is the product of admixture between populations 1 and 3. While it might be  
571 possible using other  $f$ -statistics to determine that the relationship between these populations is  
572 not well described by a pulse admixture event (LIPSON 2020), there is nothing to prevent a naïve  
573 user from attempting to model this relationship as the product of admixture using qpAdm. We  
574 therefore explore the effects of attempting to model the ancestry of population 2 (the target  
575 population) as the product of admixture between populations 1 and 3 (the source populations),  
576 with populations 0, 4, 6, 7 and 8 classified as reference populations.

577 We first consider the case of a very high migration rate ( $m=0.01$ ; equivalent to 100 migrants  
578 moving from one population to the neighboring population per generation). Out of 20 replicates,  
579 qpAdm identifies the proposed model as plausible in 90% of cases, suggesting that qpAdm cannot  
580 always distinguish between population histories that involve continuous migration and those  
581 involving pulses of admixture. Further, qpAdm assigns admixture proportions of approximately  
582 50% to each source population, which is sensible because each population does contribute  
583 roughly equal amounts of ancestry to the target population (Figure 10D-E; Supplementary Table  
584 22). When we consider lower migration rates ( $m=0.001$  and  $m=0.0001$ ) we observe similar  
585 admixture proportion estimates, but all of the p-values fall well below the 0.05 threshold,  
586 suggesting that with lower rates of migration, qpAdm will reject admixture as a plausible model  
587 when the actual history involves continuous migration.

588 These results suggest that users should be sure to consider alternative demographic models to  
589 pulse admixture, even in cases when qpAdm produces admixture proportion estimates and p-  
590 values that appear plausible. This scenario likely represents just one of many cases in which  
591 qpAdm identifies plausible admixture models for populations that were not formed via  
592 admixture, therefore, we caution that users should use additional tools, in conjunction with or  
593 prior to qpAdm analysis, to determine whether admixture is a likely demographic scenario.

## 594 DISCUSSION

595 We find that qpAdm can accurately identify plausible admixture models and estimate admixture  
596 proportions when applied to simulated data, matching previous theoretical expectations (HAAK  
597 *et al.* 2015). When an appropriate admixture model is suggested, qpAdm calculates p-values that  
598 follow a uniform distribution, suggesting that a cut off value of 0.05 will result in the acceptance  
599 of a correct model in 95% of cases. Additionally, qpAdm estimates admixture proportions with  
600 high accuracy, even when calculated on datasets with a limited number of SNPs, high rates of  
601 missingness or damage (when occurring at similar rates in all populations), or when analyses are  
602 performed on pseudo-haploid data or on data that is subject to strong ascertainment bias.  
603 Additionally, while the use of populations with small sample sizes does increase the variance in  
604 admixture proportion estimates, admixture proportion estimates appear unbiased.

605 Further, we tested two commonly used strategies for identifying the best admixture model using  
606 qpAdm—base and rotating—and find that both strategies can distinguish between plausible and  
607 implausible models. However, the rotating strategy is better able to distinguish between

608 plausible and implausible models, particularly when the potential source populations are closely  
609 related. We therefore recommend users implement a rotating model comparison strategy when  
610 possible. It is important to note that the results from qpAdm are always going to depend on the  
611 availability of samples. Thus, even if the rotating strategy points to one particular model as the  
612 optimal model for a given dataset, this should not be taken as proof that the source populations  
613 identified are the actual best sources populations. For example, in Figure 1, if data were available  
614 from population 8 and not from population 9, the rotating model would identify populations 5  
615 and 8 as the optimal sources of population 14. This would be correct, given the samples available,  
616 but it would come as no surprise if data from population 9 subsequently became available and it  
617 was deemed a better source than population 8. A number of examples exist in which previously  
618 identified qpAdm models have been refined when ancient DNA from new populations has  
619 become available, including in the Levant (HABER *et al.* 2017; HARNEY *et al.* 2018) and Sardinia  
620 (HAAK *et al.* 2015; CHIANG *et al.* 2018; FERNANDES *et al.* 2020; MARCUS *et al.* 2020).

621 While qpAdm's ability to identify the optimal admixture model is affected by data quality,  
622 including the amount of missing data, the number of individuals in an analysis population, and  
623 the rate of ancient DNA damage, none of these factors ever bias qpAdm towards accepting a  
624 non-optimal model and rejecting the optimal model. Instead, we find that high rates of missing  
625 data or small sample size may make it more likely for qpAdm to accept multiple models. On the  
626 other hand, ancient DNA damage appears to cause qpAdm to be too stringent when it occurs at  
627 differential rates in the target and optimal source populations, often rejecting models that should  
628 be considered optimal, and resulting in biased admixture proportion estimates. While these  
629 results show that improving data quality and carefully curating data prior to analysis should be a

630 priority of qpAdm users, they are promising as they suggest that data quality issues are unlikely  
631 to causes users to infer an incorrect model of admixture using qpAdm.

632 Although we find that the performance of qpAdm matches theoretical predictions under  
633 standard conditions, we also highlight several cases in which users should exercise caution. For  
634 instance, we find that users should attempt to limit the number of reference populations  
635 included in a qpAdm model, as the inclusion of too many reference populations may result in  
636 lowered p-values. Further, we show that qpAdm may produce plausible admixture proportion  
637 estimates and p-values in cases where the population of interest was not formed via admixture,  
638 such as the case of continuous migration, therefore users should be careful to consider whether  
639 alternative demographic models may better explain their data.

640 Overall, we find that qpAdm is a useful tool for identifying plausible admixture models and  
641 estimating admixture proportions, and that its performance matches theoretical expectations.  
642 qpAdm is particularly useful because it can be used in cases where the underlying population  
643 history of all the populations included in the analysis is difficult to determine and can therefore  
644 be used in cases where it may not be possible to use other tools for modeling population histories  
645 that involve admixture, like qpGraph and TreeMix. We include an updated user guide for qpAdm  
646 in Supplementary Materials 1 in order to make this method more accessible to future users.



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